

Fluid Leakage across a Pressure Seal

Ruby R P
Gaurav Kulkarni
Udayan Kanade

Mathematical Model → Simulation

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Simulation → Mathematical Model

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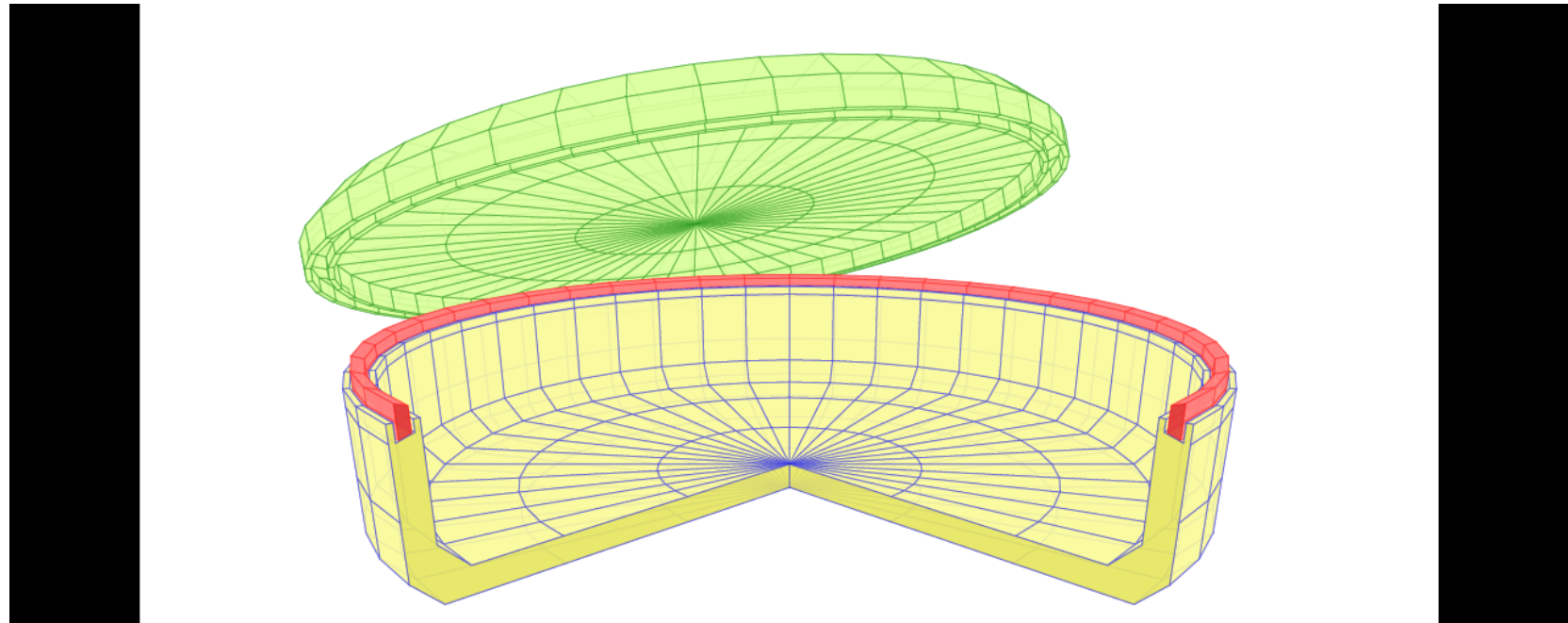
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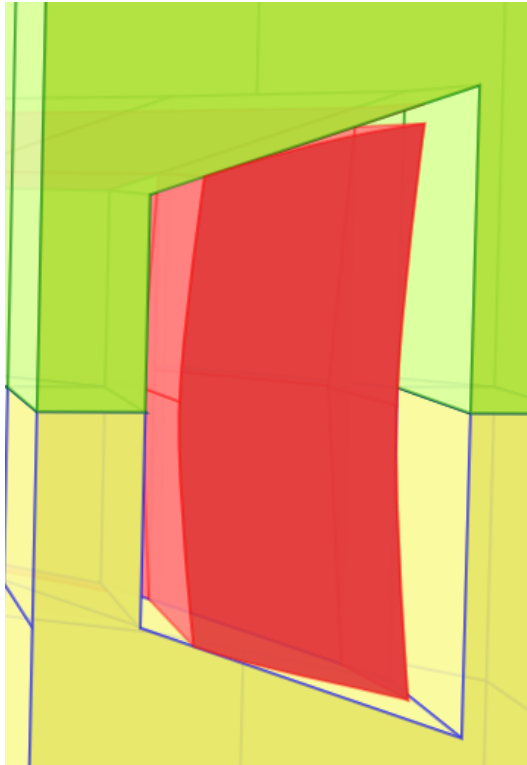
Multi-Scale Modeling (Homogenization)

- Mathematical theory of coordination between phenomena happening at different scales

Gasket Seals



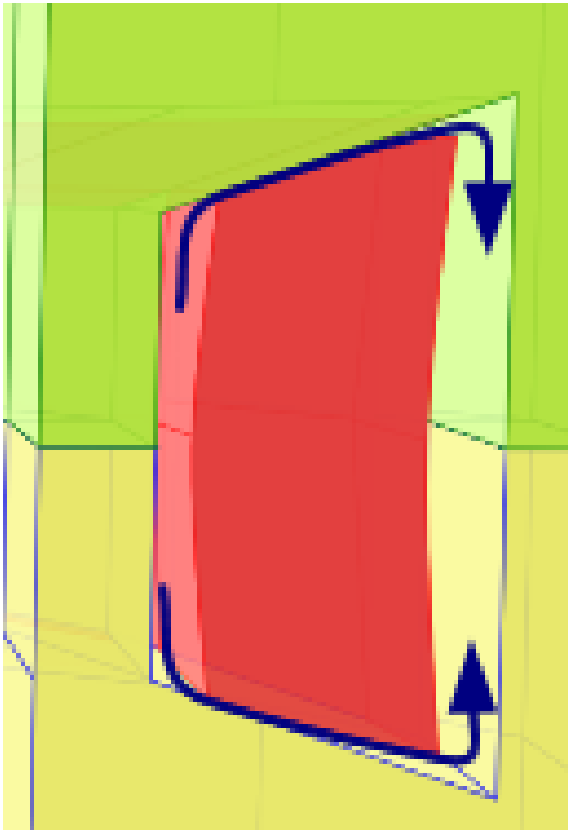
Gasket Seals



Leakage rate depends on:

- Geometries
- Materials
- Surface characteristics
- Clamping forces
- Fluid pressure

Fluid Leakage

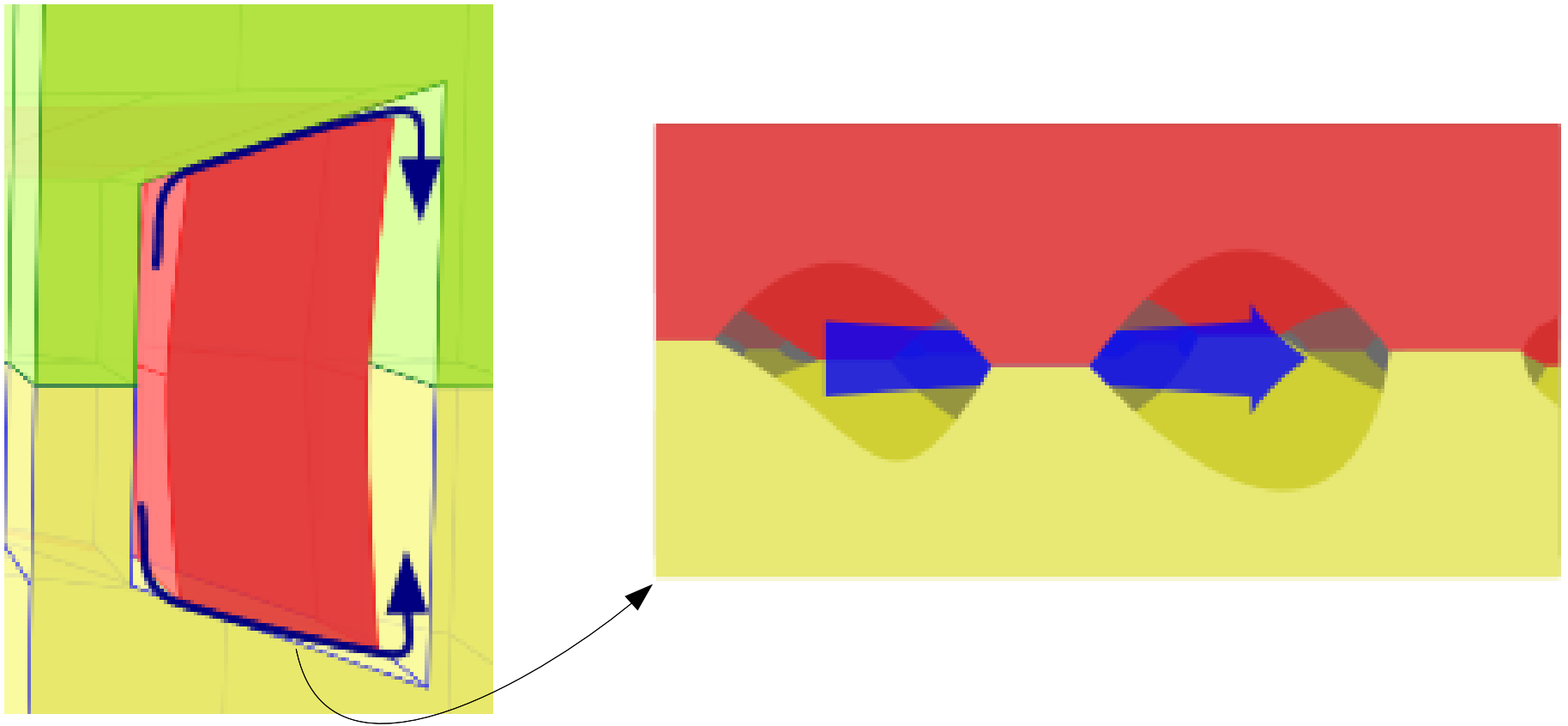


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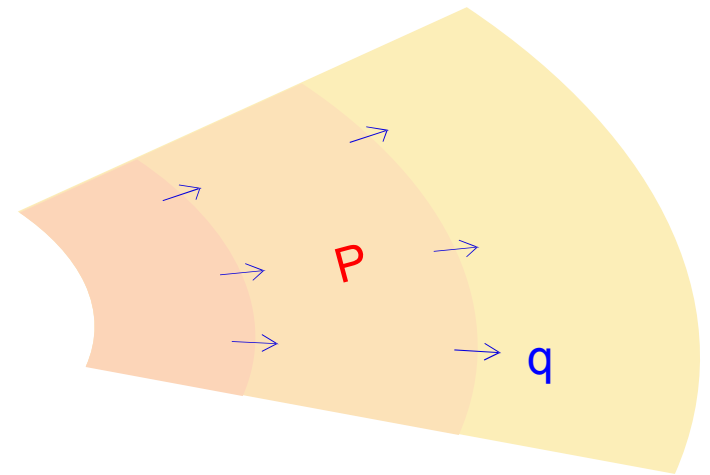
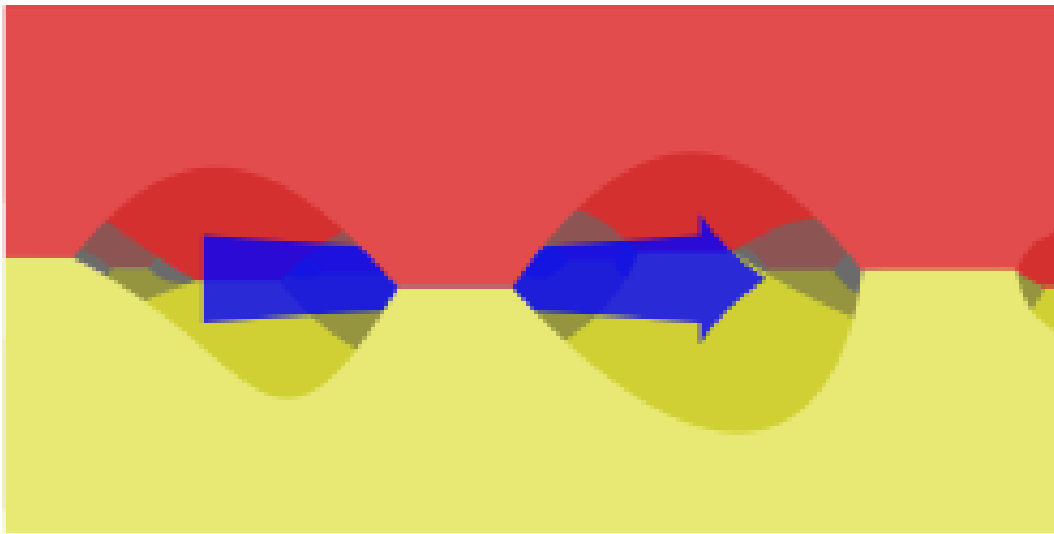
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Fluid Leakage

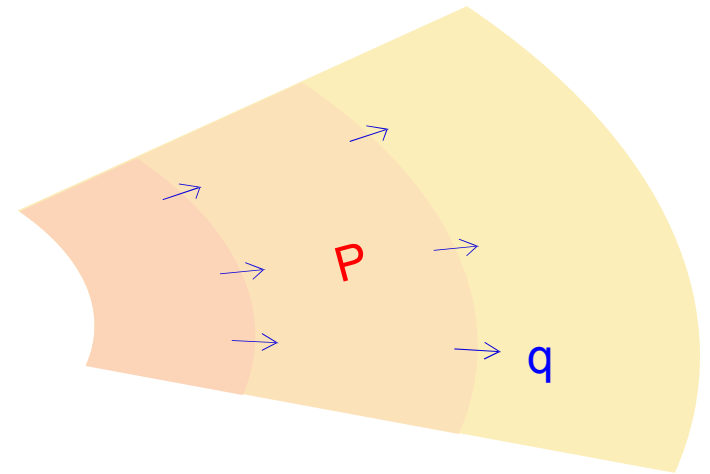


Homogenization



Homogenization

$$q = a \nabla P$$



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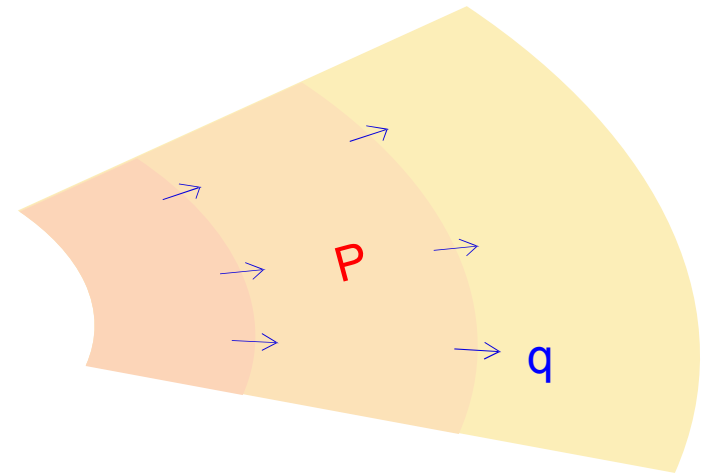
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Homogenization

$$q = a \nabla P$$

$$a = a(S, P, |\nabla P|)$$



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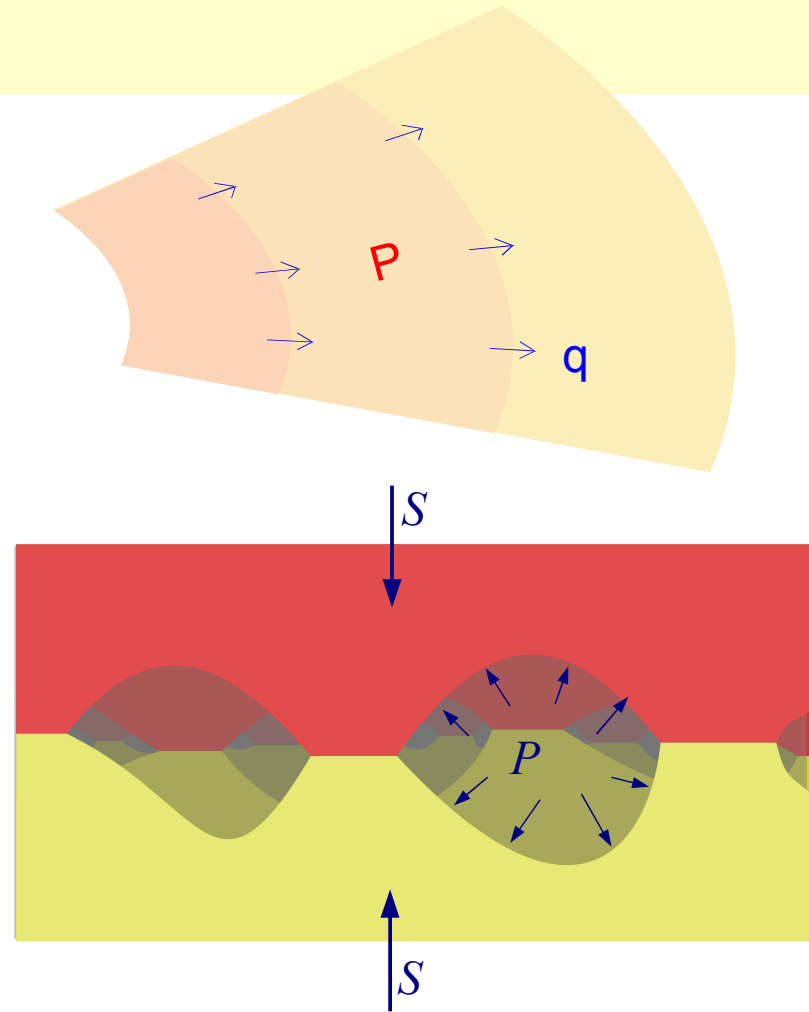
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Homogenization

$$q = a \nabla P$$

$$a = a(S, P, |\nabla P|)$$



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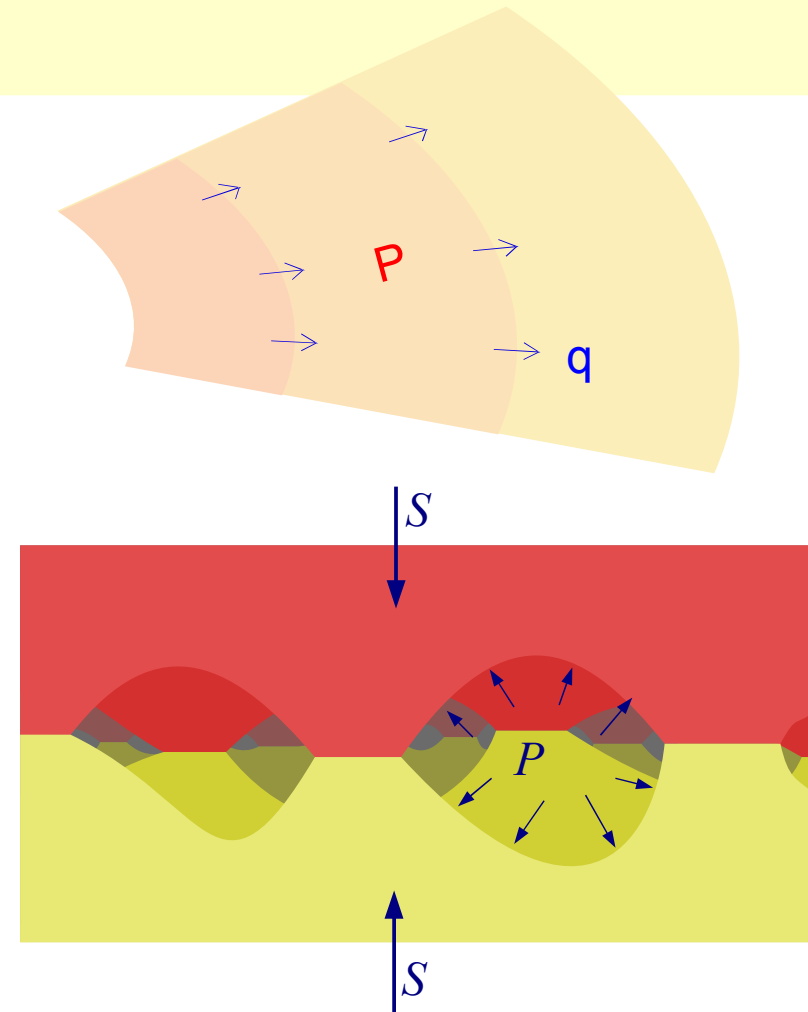
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Geometric Result

$$q = a \nabla P$$

$$a = a(S, P, |\nabla P|)$$

Geometry of
microcaverns depends
only on $S - P$



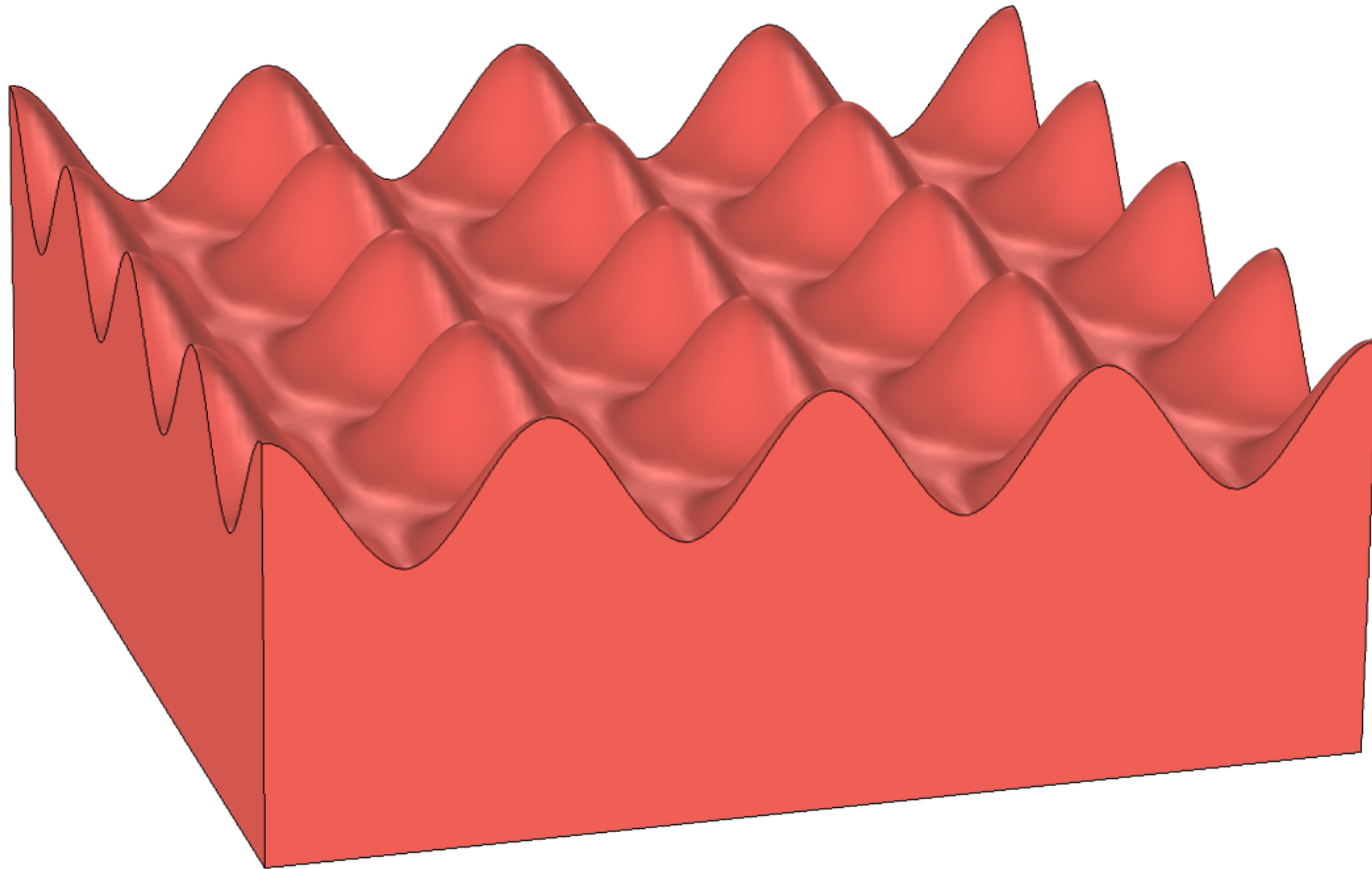
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Idealization

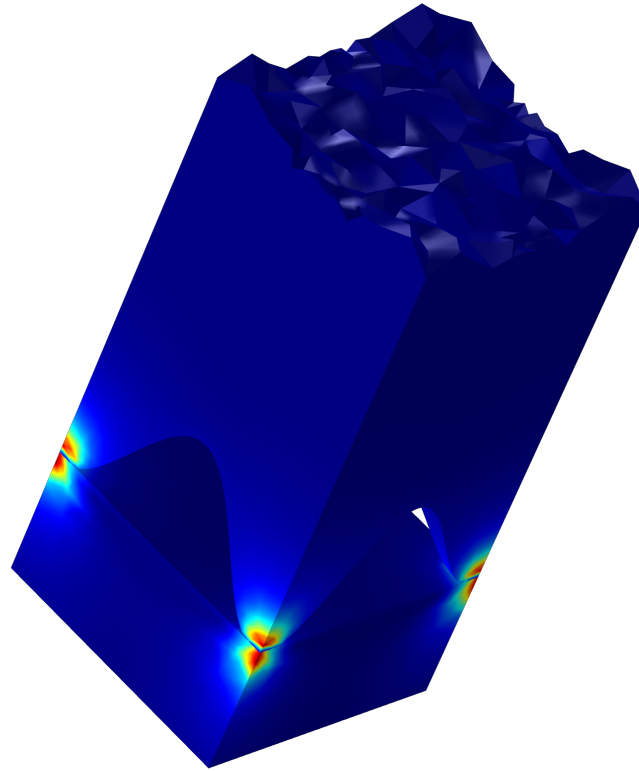


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Mechanical Simulation



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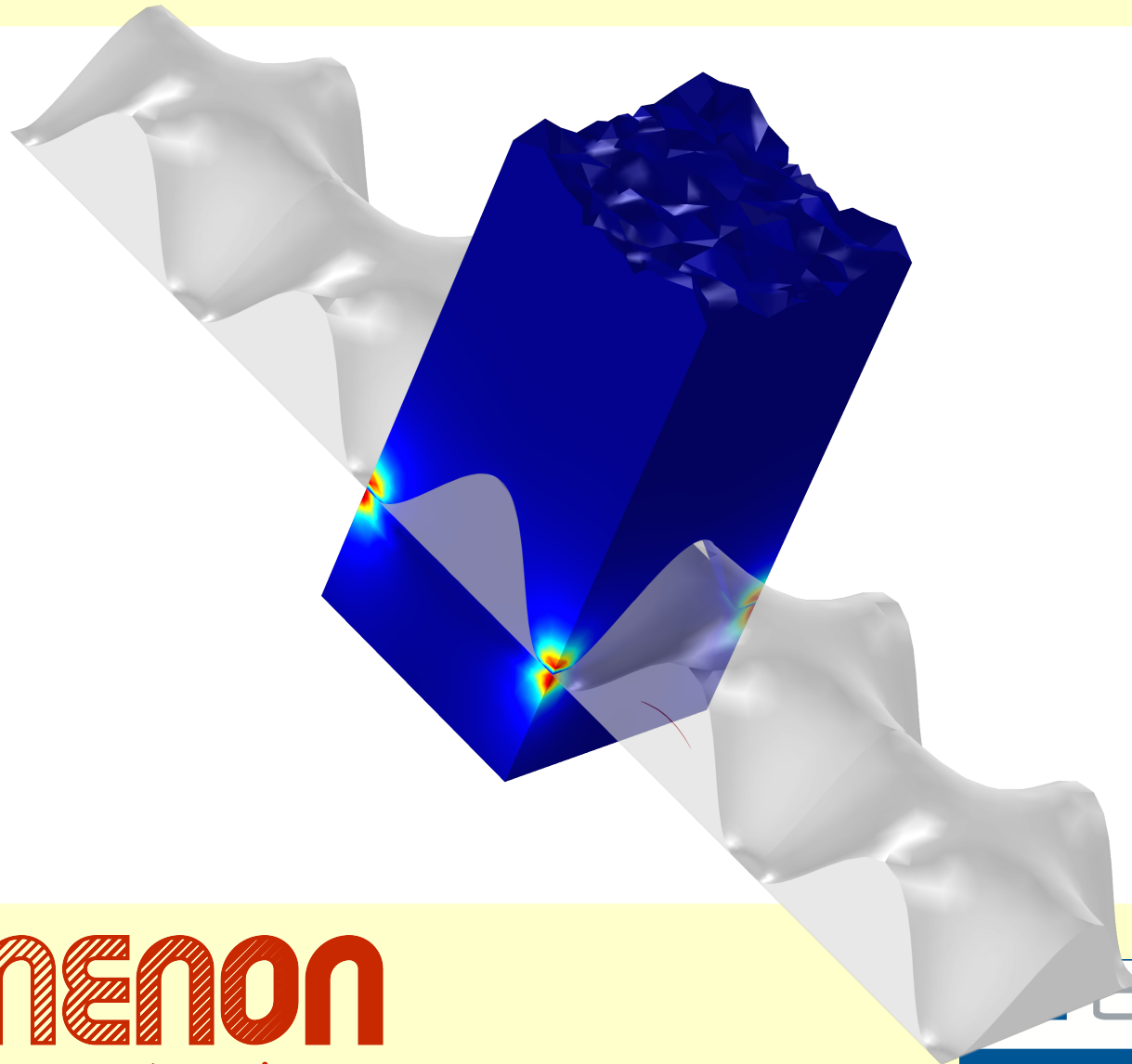
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Fluid Domain



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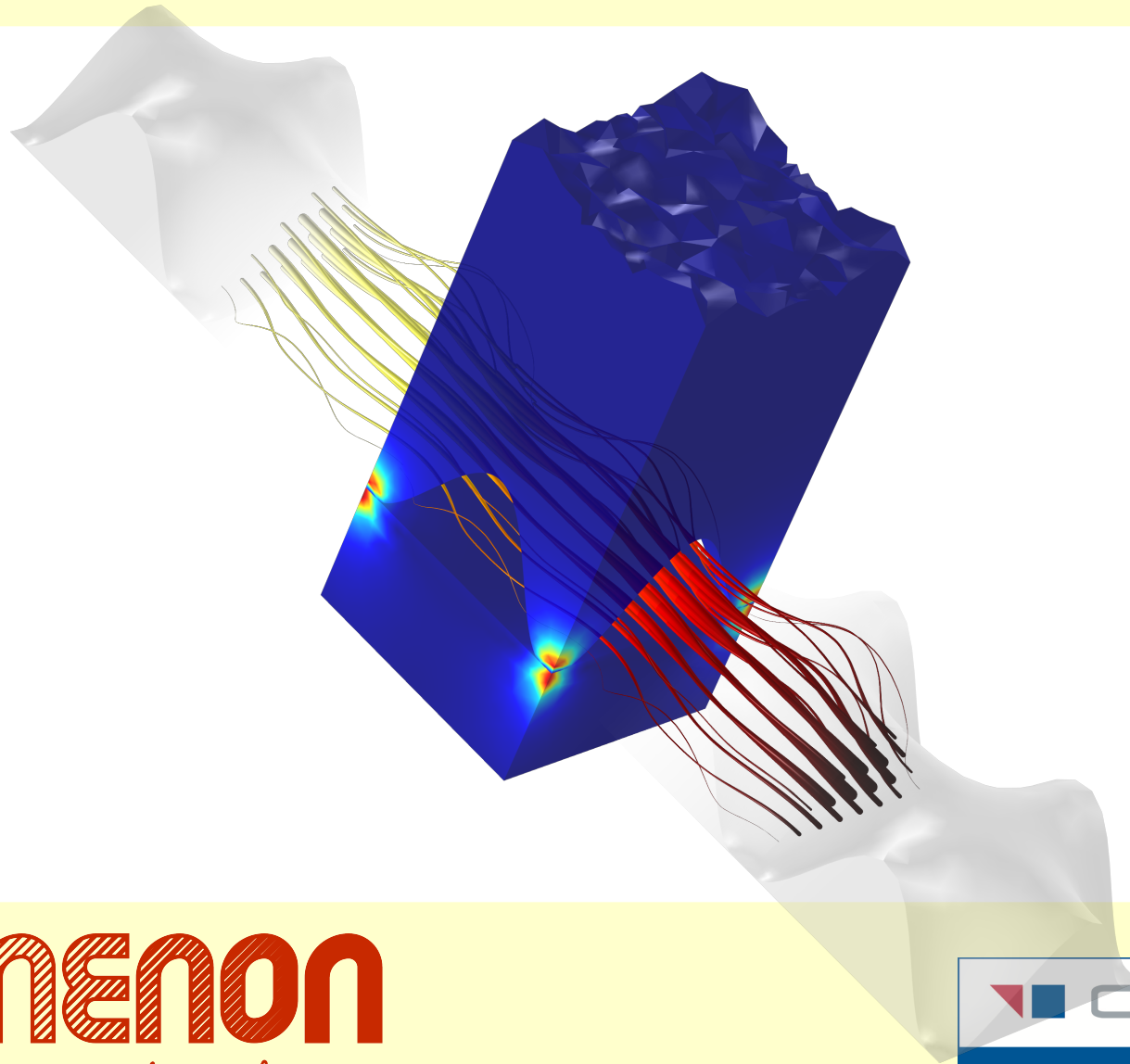
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Fluid Flow



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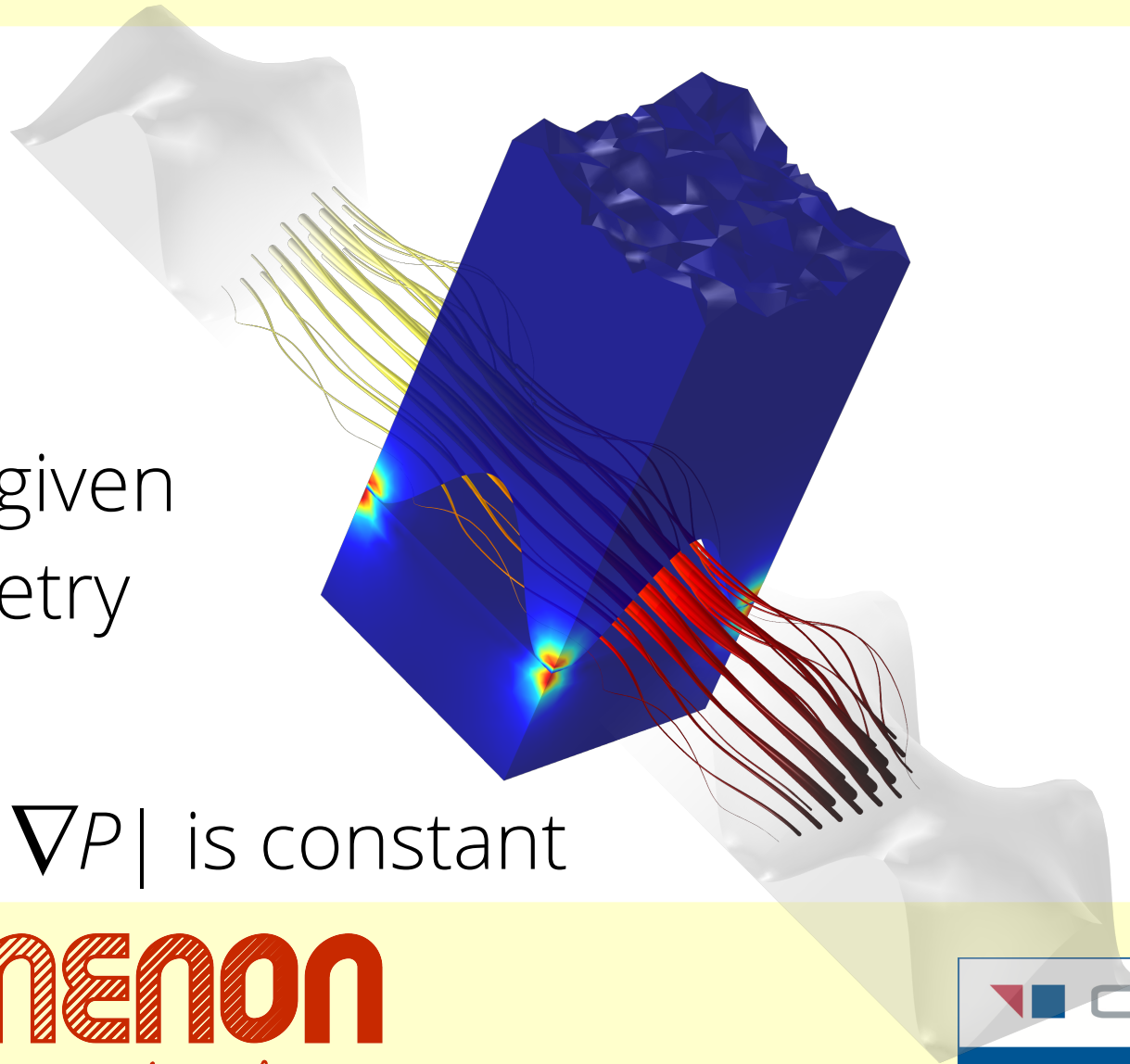
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Correlation

For a given geometry

- $q / P |\nabla P|$ is constant



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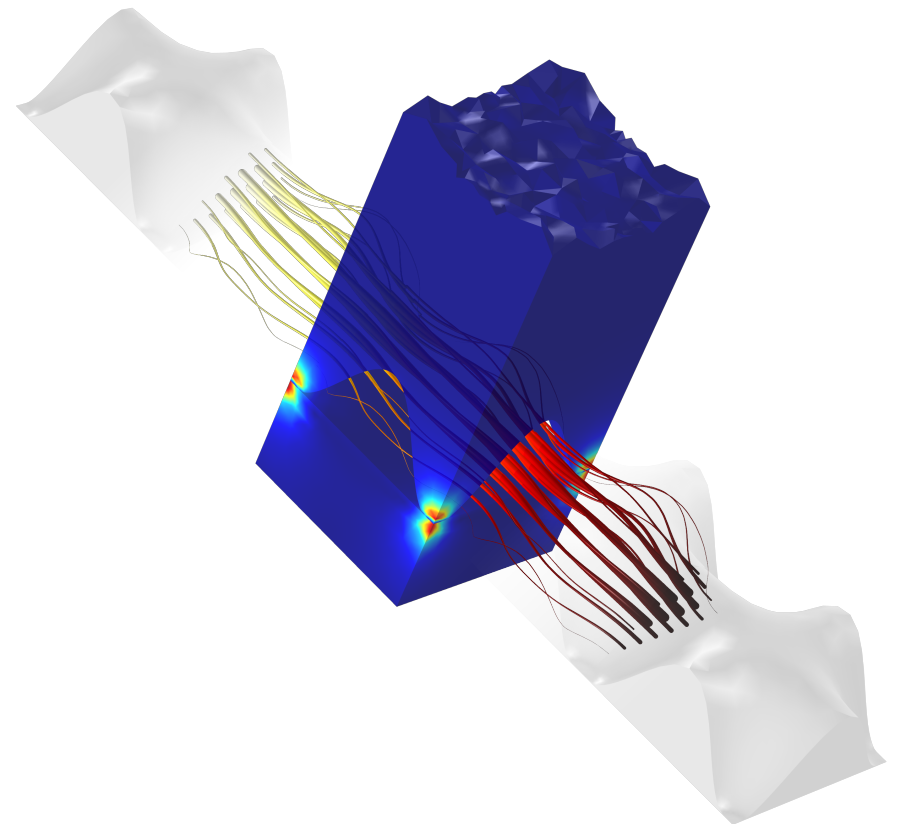
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New Formula

- $q = f(S - P) P |\nabla P|$

For a given geometry

- $q / P |\nabla P|$ is constant



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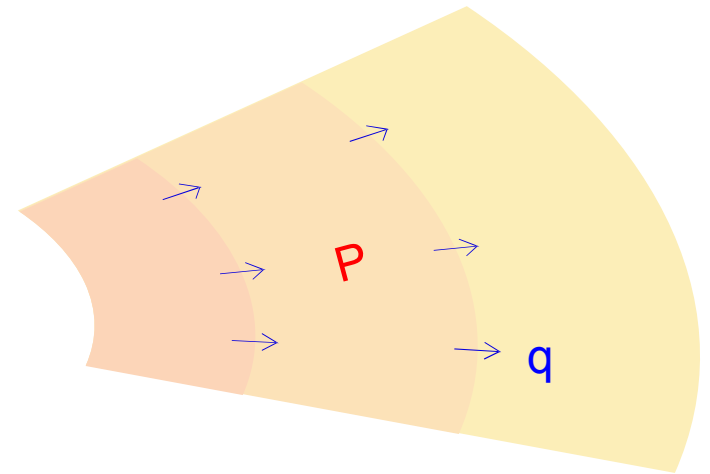
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New PDE!!!

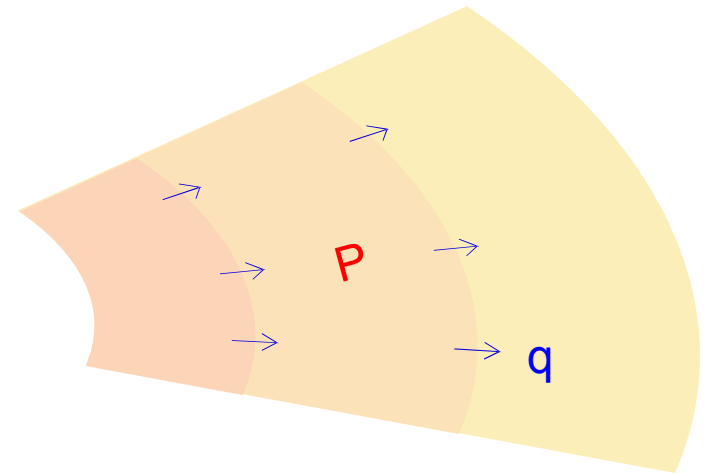
- $q = f(S - P) P |\nabla P|$



New PDE!!!

- $q = f(S - P) P |\nabla P|$

- $\nabla \cdot q = 0$



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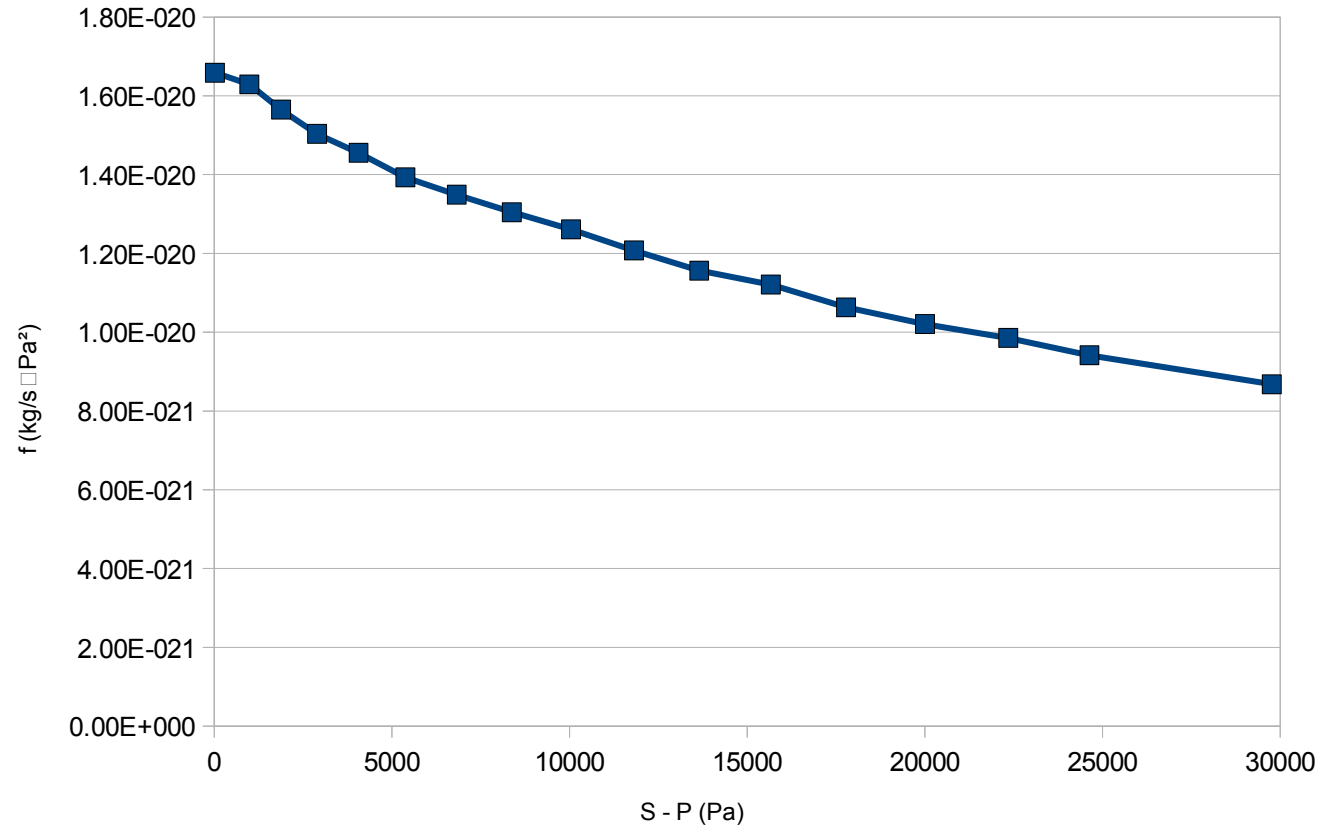
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$$q = f(S - P) P |\nabla P|$$

Conductance parameter f as a function of S-P



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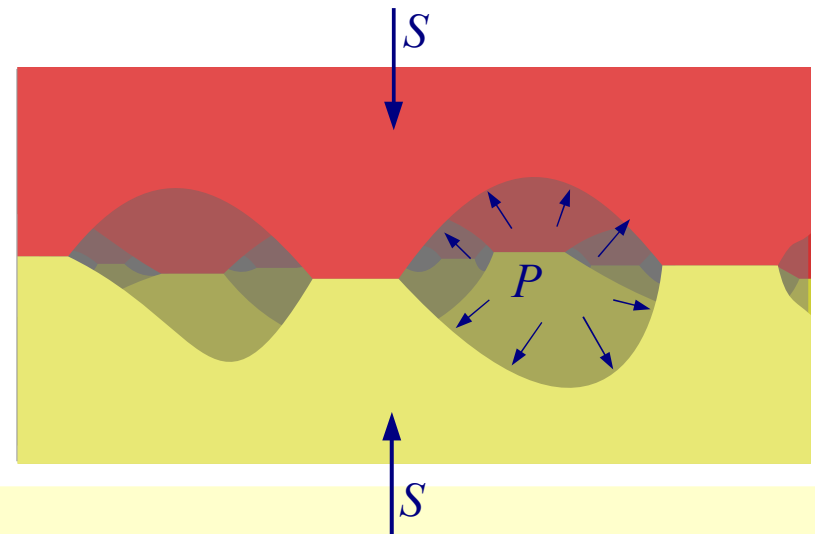
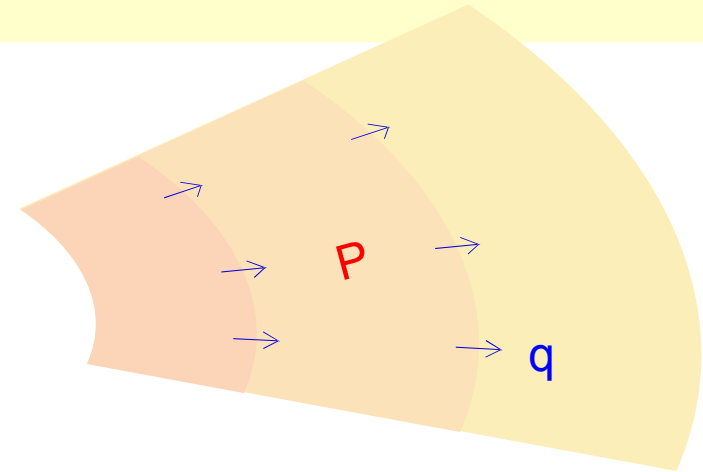
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What we have achieved

$$q = a(S, P, |\nabla P|) \nabla P$$

- $q = f(S - P) P |\nabla P|$

$$\nabla \cdot q = 0$$



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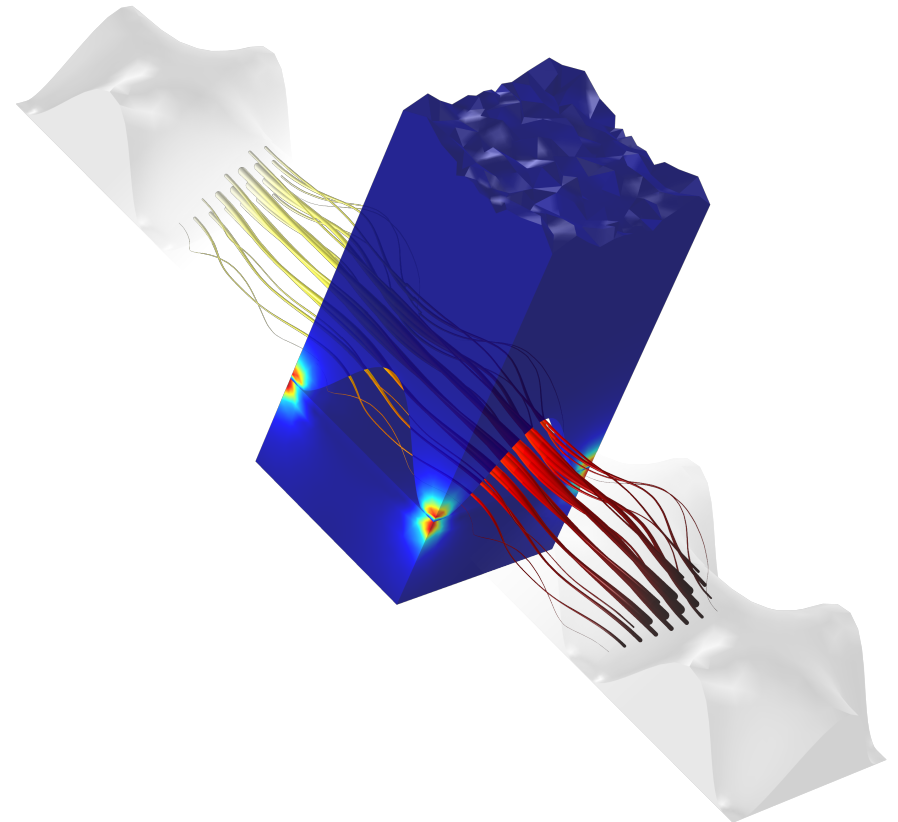
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Thank you!

$$q = a(S, P, |\nabla P|) \nabla P$$

- $q = f(S - P) P |\nabla P|$

$$\nabla \cdot q = 0$$



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